

(Q1) Design a simply supported roof slab for a room $7.5\text{m} \times 3.5\text{m}$ clear in size. The slab is carrying an imposed load of 5KN/m^2 . Use M20 grade and Fe415 steel.

Sol:- Given data :- size of slab = $7.5\text{m} \times 3.5\text{m}$, live load = 5KN/m^2

$$\text{live load} = 5\text{KN/m}^2$$

$$\frac{l_y}{l_x} = \frac{7.5}{3.5}$$

Design the one slab [d, A_{st}] $> 2 \rightarrow$ design as one way slab

Assuming total depth = $D = 150\text{mm}$

(i) Effective depth, $d = D - \text{clear cover} - \frac{\phi}{2}$

$$d = 150 - 20 - \frac{10}{2}$$

$$d = 125\text{mm}$$

(ii) Effective span (l_{eff}) :-

(a) $l_{eff} = \text{clear span} + \text{width of support}$

$$l_{eff} = \text{clear span} + d$$

which ever is less

Assume support width = $200\text{mm} = 0.2\text{m}$

or $l_{eff} = 3.5 + 0.2 = 3.7\text{m}$

$$= 3.5 + 0.125 = 3.625\text{m}$$

adopt, $l_{eff} = 3.625\text{m}$

(2) Factored Bending Moment: M_{ud} :-

load for 1m width of slab :-

$$\text{Self wt. of slab} = b \times D \times 25$$

$$= 1 \times 0.15 \times 25 = 3.75 \text{ KN/m}$$

$$\text{Live load} = 5 \text{ KN/m}$$

$$\text{Total load} = 5 + 3.75 = 8.75 \text{ KN/m}$$

$$\text{Design load, } w_u = 1.5 \times 8.75 = 13.125 \text{ KN/m}$$

$$\text{Factored Moment, } M_{ud} = \frac{w_u l_{eff}^2}{8} = \frac{13.125 \times (3.525)^2}{8}$$

$$= 21.60 \text{ KN-m}$$

$$\text{Factored Shear force, } V_u = \frac{w_u l}{2} = \frac{13.125 \times 3.5}{2}$$

$$= 22.97 \text{ KN}$$

③ check for effective depth: d :

$$d = \sqrt{\frac{M_u}{0.36 f_{ck} b}}$$

$$M_{ud} = 0.36 f_{ck} b x_{max} (d - 0.42 x_{max})$$

$$M_{ud} = 0.36 f_{ck} b \times 0.48d (d - 0.42 \times 0.48d)$$

$$M_{ud} = 0.36 f_{ck} b \times 0.48d^2 (1 - 0.42 \times 0.48)$$

$$d^2 = \frac{M_{ud}}{0.36 f_{ck} b \times 0.48 (1 - 0.42 \times 0.48)}$$

$$d = \sqrt{\frac{M_{ud}}{0.36 \times 20 \times 1000 \times 0.48 (1 - 0.42 \times 0.48)}} = \sqrt{\frac{21.6 \times 10^6}{2.}}$$

$$d = \sqrt{\frac{21.6 \times 10^6}{0.36 \times 20 \times 1000 \times 0.48 (1 - 0.42 \times 0.48)}}$$

$$d = 88.5 \text{ mm} < 125 \text{ mm} \quad (\text{OK})$$

④ Area of tensile steel: A_{st} (1% raw reinforcement)

$$M_{ud} = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{b d f_{ck}} \right]$$

$$21.6 \times 10^6 = 0.87 \times 415 A_{st} \left[1 - \frac{A_{st} \times 415}{1000 \times \phi 25 \times 20} \right]$$

$$21.6 \times 10^6 = 361.05 A_{st} - 0.06 A_{st}^2$$

$$A_{st}^2 - 6024 A_{st} + 21.6 \times 10^6 = 0$$

$$21.6 \times 10^6 = 45131.25 A_{st} - 7.49 A_{st}^2$$

$$7.49 A_{st}^2 - 45131.25 A_{st} + 21.6 \times 10^6 = 0$$

$$A_{st} = 524.2 \text{ mm}^2$$

using 10mm diameter bars

$$\text{Spacing of bars} = \frac{1000 \times \text{Area of one bar}}{A_{st}}$$

$$= \frac{1000 \times \frac{\pi}{4} (10)^2}{524.2} = 150 \text{ mm}$$

Provide 10mm ϕ diameter bar @ 150mm c/c spacing

Bent up of alternate bars at $\frac{l_{eff}}{7} = \frac{3625}{7} = 517\text{mm} \approx 520\text{mm}$ from face of support

⑤ Distribution steel: Distribution steel is provided in longer direction

= 0.12% of cross sectional area

$$= \frac{0.12}{100} \times bD = \frac{0.12}{100} \times 1000 \times 150$$

$$= 180\text{mm}^2$$

using 6mm ϕ bar

$$\text{Spacing} = \frac{1000 \times \frac{\pi}{4} (6)^2}{180} = 157.22\text{mm} \leq 150\text{mm c/c}$$

Provide 6mm ϕ bar @ 150mm c/c in the longer direction

⑥ check for shear:

i) Factored shear force = $V_u = 22970\text{ kN}$

Nominal shear stress, $\tau_{sr} = \frac{V_u}{bd} = \frac{22970}{1000 \times 125} = 0.184\text{ N/mm}^2$

Design shear strength of concrete τ_c

$$p_t = \frac{100 \times A_{st}/2}{bd} = \frac{100 \times 524.2/2}{1000 \times 125} = 0.21\%$$

$$\tau_c = 0.28 + \left(\frac{0.36 - 0.28}{0.25 - 0.15} \right) (0.21 - 0.15)$$

$$= 0.328 \text{ N/mm}^2$$

$\tau_v < \tau_c \rightarrow$ hence the design is safe in shear

⑦ check for deflection:

$$p_t = \frac{100 A_{st}}{bd} = \frac{100 \times 524.2}{1000 \times 125} = 0.42\%$$

$$f_s = 0.58 f_y \left[\frac{A_{st \text{ required}}}{A_{st \text{ provided}}} \right]$$

$$= 0.58 \times 415 \left[\frac{524.2}{524.2} \right] = 240 \text{ N/mm}^2$$

for $p_t = 0.42\%$, $f_s = 240 \text{ N/mm}^2$, $R_t = 1.55$

$$\left(\frac{l}{d} \right)_{\text{max}} = 20 \times R_t = 20 \times 1.55 = 31$$

$$\left(\frac{l_{\text{eff}}}{d} \right)_{\text{provided}} = \frac{3625}{125} = 29$$

$\left(\frac{l}{d} \right)_{\text{max}} > \left(\frac{l}{d} \right)_{\text{provided}}$, Hence the design is safe in deflection.

⑧ check for development length :

SLAB

Moment of resistance at support by 10mm diameter bar @ 300mm/c/c

$$\text{Reinforcement at support} = \frac{524.2}{2} = 262.1 \text{ mm}^2$$

$$M_r = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{b d f_{ck}} \right]$$

$$M_r = 0.87 \times 415 \times 262.1 \left[1 - \frac{262.1 \times 415}{1000 \times 125 \times 20} \right]$$

$$= 11.31 \times 10^6 \text{ N-mm}$$

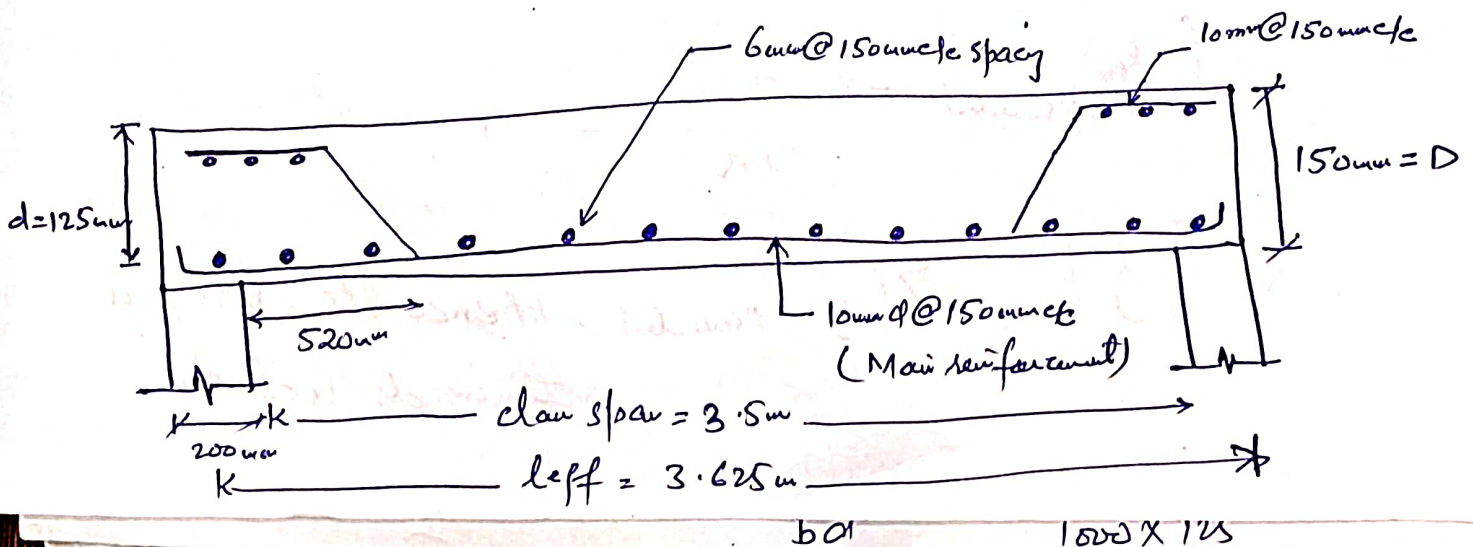
Factored shear force, $V_u = 22970 \text{ N}$

Providing no hooks, $l_o = 0$

$$\frac{M_r}{V} + l_o = \frac{11.31 \times 10^6}{22970} + 0 = 492 \text{ mm}$$

$$L_d = \frac{0.87 f_y \phi}{4 \tau_{bd}} = \frac{0.87 \times 415 \times 10}{4 \times 1.2 \times 1.6} = 470 \text{ mm}$$

$\frac{M_r}{V_u} + l_o > L_d \rightarrow$ Hence slab is safe



Two way slab: When the ratio of $\frac{l_y}{l_x} \leq 2$, then the slab ~~is~~ will be designed as ~~two~~ way slab.

(a) Two way slab with corners not held down / free to lift

(b) Two " " " " held down / prevent to lift

(Q2): Design a Simply Supported slab for a room $4000\text{mm} \times 3500\text{mm}$ clear in size if the Superimposed load is 3KN/m^2 and floor finish of 1KN/m^2 . The edges of the slab are not held down. Use M20 grade concrete and Fe 415 steel?

Sol:-

$$\frac{l_y}{l_x} = \frac{4}{3.5} = 1.14 < 2$$

Hence, the slab is to be designed as a two way slab.

1) Given Data:-

- Shorter span, $l_x = 3.5\text{m}$
- Long span, $l_y = 4\text{m}$
- Live load = 3KN/m^2
- Floor finish = 1KN/m^2
- $f_{ck} = 20\text{N/mm}^2$
- $f_y = 415\text{N/mm}^2$

2) Thickness of slab:

Assume effective depth, $d =$

Assume % of steel, $p_t = 0.2\%$

$d = 20$ [Simply supported slab]

Modification factor, $\gamma = 1.68$

$$\left(\frac{L}{d}\right) = \alpha \cdot \gamma$$

$$\frac{3.5 \times 10^3}{d} = 20 \times 1.68$$

$$\frac{3500}{20 \times 1.68} = d$$

$$\boxed{104.2 \text{ mm} = d}$$

Take, $d = 105 \text{ mm}$

$$\text{Total depth, } D = d + 20 + \frac{\phi}{2}$$

$$D = 105 + 20 + \frac{10}{2} = 130 \text{ mm}$$

③ Effective span: $(l_x)_{\text{eff}}$

$$(l_x)_{\text{eff}} = \text{clear span} + \text{width of support}$$

$$\text{or } = \text{clear span} + d$$

$$(l_x)_{\text{eff}} = 3.5 + 0.3 \quad [\text{Assumed width of support} = 300 \text{ mm}]$$

$$= 3.8 \text{ m}$$

$$(l_x)_{\text{eff}} = 3.5 + 0.105 = 3.605 \text{ m}$$

$$\text{Adopt, } (l_x)_{\text{eff}} = 3.605 \text{ m}$$

④ Loads: load per unit area of slab.

$$\text{Self wt. of slab} = \cancel{0.13} \cdot 0.13 \times 25 = 3.25 \text{ KN/m}^2$$

$$\text{Live load} = 3 \text{ KN/m}^2$$

$$\text{floor finish load} = 1 \text{ KN/m}^2$$

$$\text{Total load} = 7.25 \text{ KN/m}^2$$

$$\text{Total load/m} = 7.25 \times 1 = 7.25 \text{ KN/m}$$

$$\text{Factored load, } W_u = 1.5 \times 7.25 = 10.875 \text{ KN/m}$$

⑤ Design Moments: $\left[\frac{l_y}{l_x} = 1.14 \right]$

$$\alpha_x = 0.074 + \left(\frac{0.084 - 0.074}{1.2 - 1.1} \right) \times (1.14 - 1.1)$$

$$= 0.078$$

$$\alpha_y = 0.061 - \left(\frac{0.061 - 0.059}{1.2 - 1.1} \right) (1.14 - 1.1)$$

$$\alpha_y = 0.06$$

$$\begin{aligned} M_{ux} &= \alpha_x w l_x^2 = 0.078 \times 10.875 \times (3.605)^2 \\ &= 11.02 \text{ KN-m} \end{aligned}$$

$$\begin{aligned} M_{uy} &= \alpha_y w l_x^2 = 0.06 \times 10.875 \times (3.605)^2 \\ &= 8.48 \text{ KN-m} \end{aligned}$$

⑥ Minimum depth required:

$$M_{uo} = 0.36 f_{ck} b x_{u, \max} (d - 0.42 x_{u, \max})$$

$$11.02 \times 10^6 = 0.36 \times 20 \times 1000 \times 0.48 \times d (d - 0.42 \times 0.48 d)$$

$d = 68.2 \text{ mm} < 105 \text{ mm}$, Hence, the design is safe.

⑦ Reinforcement^{in Middle strip}: Along shorter direction

$$M_{ux} = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{b d f_{ck}} \right]$$

$$11.02 \times 10^6 = 0.87 \times 415 A_{st} \times 105 \left[1 - \frac{A_{st} \times 415}{1000 \times 105 \times 20} \right]$$

$$11.02 \times 10^6 = 37910.25 A_{st} - 7.49 A_{st}^2$$

$$7.49 A_{st}^2 - 37910.25 A_{st} + 11.02 \times 10^6 = 0$$

$$A_{st} = 309.63 \text{ mm}^2$$

using 8mm ϕ bars.

$$\text{c/c Spacing of bars} = \frac{1000 \times \frac{\pi}{4} \times (8)^2}{309.63} = 162.34 \text{ mm}$$

$\approx 160 \text{ mm c/c}$

Max spacing (i) $3d = 3 \times 105 = 315$ or 300mm (whichever is less)

Hence, provide 8mm ϕ @ ~~160~~¹⁶⁰ mm c/c Spacing along shorter direction

Along longer direction: effective depth for longer direction.

$$d = 105 - 8 = 97 \text{ mm}$$

$$M_{uy} = 0.87 f_y A_{st} d \left[1 - \frac{A_{st} f_y}{b d f_{ck}} \right]$$

$$8.48 \times 10^6 = 0.87 \times 415 A_{st} \times 97 \left[1 - \frac{A_{st} \times 415}{1000 \times 97} \times \frac{415}{20} \right]$$

$$8.48 \times 10^6 = 35021.85 A_{st} - 7.49 A_{st}^2$$

$$7.49 A_{st}^2 - 35021.85 A_{st} + 8.48 \times 10^6 = 0$$

$$A_{st} = 256.2 \text{ mm}^2$$

using 8mm bars

$$\text{c/c spacing} = \frac{1000 \times \frac{\pi}{4} (8)^2}{256.2} = 196.2 \text{ mm}$$

Max spacing, (i) $3d = 3 \times 105 = 315 \text{ mm}$, (ii) 300 mm (whichever is less)

Hence, provide 8mm ϕ @ 190mm c/c spacing along longer direction

⑧ Reinforcement in edge strip:

$$A_{st} = 0.12\% \text{ of } bD = \frac{0.12}{100} \times 1000 \times 130 = 156 \text{ mm}^2$$

$$\text{using 8mm } \phi \text{ bars, spacing of bars} = \frac{1000 \times \frac{\pi}{4} (8)^2}{156} = 181.2 \text{ mm}$$

$$\begin{array}{l} \text{(i) } 5d = 5 \times 105 = 525 \text{ mm} \\ \text{(ii) } 450 \text{ mm} \end{array} \left. \begin{array}{l} \\ \end{array} \right\} \begin{array}{l} \text{whichever is} \\ \text{less} \end{array} \leq 180 \text{ mm c/c}$$

Hence, provide 8mm ϕ @ 180mm c/c spacing in edge strip

⑨ Width of edge strip:

$$\begin{array}{l} \text{width of edge strip along shorter direction} = \frac{l_x}{8} = \frac{3500}{8} = 437.5 \text{ mm} \\ \text{" " " " " longer " " } = \frac{l_y}{8} = \frac{4000}{8} = 500 \text{ mm} \end{array}$$

length of middle strip along shorter direction = $\frac{3}{4} l_n = \frac{3}{4} \times 3500$
 $= 2625 \text{ mm}$

" " " " " longer direction = $\frac{3}{4} l_y = \frac{3}{4} \times 4000 = 3000 \text{ mm}$

⑨ check for deflection:-

$\left(\frac{l}{d}\right)_{\text{max}} = 1.68 \times 20 = 33.6$

$P_t = \frac{\pi}{4} (8)^2 \times 100$
~~160~~ 160×105

$\left(\frac{l}{d}\right)_{\text{provided}} = \frac{3605}{105} = 34.33$

$P_t = 0.3\%$

Hence, the slab is not safe in deflection
 so, increase the depth of slab and redesign the slab.

$f_s = 0.58 f_y = 0.58 \times 415$
 $= 240 \text{ N/mm}^2$

$\gamma = 1.68$

